

Class 12th Mathematics

1. D.C.'s of two lines are (l_1, m_1, n_1) and (l_2, m_2, n_2) then D.C.'s of the line perpendicular to both lines are
- (a) $(m_1n_2 - m_2n_1, n_1l_2 - n_2l_1, m_2l_1 - l_2m_1)$ (b) $(l_1 + l_2, m_1 + m_2, n_1 + n_2)$
- (c) $(l_1 - l_2, m_1 - m_2, n_1 - n_2)$ (d) none of these
2. The equation of the line passing through the point $(1, 2, 3)$ and perpendicular to $x + 2y - 5z + 9 = 0$ is
- (a) $\frac{x-1}{1} = \frac{y-2}{2} = \frac{z-3}{-5}$ (b) $\frac{x-1}{1} = \frac{y-2}{2} = \frac{z+5}{3}$
- (c) $\frac{x+1}{1} = \frac{y+2}{2} = \frac{z+3}{-5}$ (d) $\frac{x+1}{1} = \frac{y+2}{2} = \frac{z-5}{3}$
3. The length of the perpendicular from the origin to the plane passing through the point \vec{a} and containing the line $\vec{r} = \vec{b} + \lambda\vec{c}$ is
- (a) $\frac{[\vec{a} \vec{b} \vec{c}]}{[\vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a}]}$ (b) $\frac{[\vec{a} \vec{b} \vec{c}]}{[\vec{a} \times \vec{b} + \vec{b} \times \vec{c}]}$
- (c) $\frac{[\vec{a} \vec{b} \vec{c}]}{[\vec{b} \times \vec{c} + \vec{c} \times \vec{a}]}$ (d) $\frac{[\vec{a} \vec{b} \vec{c}]}{[\vec{c} \times \vec{a} + \vec{a} \times \vec{b}]}$
4. The vertices of a tetrahedron are $O(0,0,0)$, $A(1, 2, 1)$, $B(2,1,3)$ and $C(-1, 1, 2)$, the angle between faces OAB and ABC is
- (a) $\cos^{-1}\left(\frac{19}{35}\right)$ (b) $\cos^{-1}\left(\frac{17}{31}\right)$ (c) 30° (d) 90°
5. A line joining points $(4, -1, 2)$ and $(-3, 2, 3)$ meets the plane at the point $(-10, 5, 4)$ at 90° , then equation of the plane is
- (a) $7x - 3y - z + 89 = 0$ (b) $7x + 3y + z + 89 = 0$
- (c) $7x - 3y + z + 89 = 0$ (d) none of these
6. A line passes through two points $A(2, -3, -1)$ and $B(8, -1, 2)$. The coordinates of a point on this line at a distance of 14 units from A are
- (a) $(14, 1, 5)$ (b) $(-10, -7, -7)$ (c) $(86, 25, 41)$ (d) none of these
7. The ratio in which yz plane cuts the line joining the point $(-2, 4, 7)$ and $(3, -5, 8)$ is
- (a) 2: 3 (b) 3: 2 (c) -2:3 (d) 4:-3
8. The angle between lines whose D.C.'s satisfy the following equations $l + m + n = 0$, $l^2 + m^2 - n^2 = 0$ is
- (a) $\frac{2\pi}{3}$ (b) $\frac{\pi}{6}$ (c) $\frac{5\pi}{6}$ (d) $\frac{\pi}{3}$
9. If O is the origin and A is any point (a,b,c) the equation of plane passing through A and perpendicular to OA is
- (a) $a(x - a) - b(y - b) - c(z - c) = 0$ (b) $a(x + a) + b(y + b) + c(z + c) = 0$
- (c) $a(x - a) + b(y - b) + c(z - c) = 0$ (d) none of these

10. The equation of the plane which passes through the points $(2, 3, -4)$ and $(1, -1, 3)$ and parallel to x -axis is
 (a) $7y - 4z - 5 = 0$ (b) $4y - 7z - 5 = 0$
 (c) $4y + 7z + 5 = 0$ (d) $7y + 4z - 5 = 0$
11. The vector equation of plane passing through three non-collinear points having position vectors $\vec{a}, \vec{b}, \vec{c}$
 (a) $\vec{r} \cdot (\vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a}) = 0$ (b) $\vec{r} \times (\vec{a} \times \vec{b} + \vec{b} \times \vec{c}) = [\vec{a} \vec{b} \vec{c}]$
 (c) $\vec{r} \cdot (\vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a}) + [\vec{a} \vec{b} \vec{c}] = 0$ (d) none of these
12. The vector equation of the plane through the point $2\hat{i} - \hat{j} - 4\hat{k}$ and parallel to the plane $\vec{r} \cdot (4\hat{i} - 12\hat{j} - 3\hat{k}) - 7 = 0$ is
 (a) $\vec{r} \cdot (4\hat{i} - 12\hat{j} - 3\hat{k}) = 0$ (b) $\vec{r} \cdot (4\hat{i} - 12\hat{j} - 3\hat{k}) = 32$
 (c) $\vec{r} \cdot (4\hat{i} - 12\hat{j} - 3\hat{k}) = 12$ (d) none of these
13. A straight line $\vec{r} = \vec{a} + \lambda \vec{b}$ meets the plane $\vec{r} \cdot \vec{n} = 0$ in P . The position vector of P is
 (a) $\vec{a} + \left(\frac{\vec{a} \cdot \vec{n}}{\vec{b} \cdot \vec{n}} \right) \vec{b}$ (b) $\vec{a} - \left(\frac{\vec{a} \cdot \vec{n}}{\vec{b} \cdot \vec{n}} \right) \vec{a}$ (c) $\vec{a} - \left(\frac{\vec{a} \cdot \vec{n}}{\vec{b} \cdot \vec{n}} \right) \vec{b}$ (d) none of these
14. A line makes angles $\alpha, \beta, \gamma, \delta$ with four diagonals of a cube then, $\cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma + \cos^2 \delta =$
 (a) $\frac{2}{3}$ (b) $\frac{4}{3}$ (c) $\frac{8}{3}$ (d) $\frac{1}{3}$
15. If $\vec{a}, \vec{b}, \vec{c}$ are three non-coplanar vectors such that $\vec{r}_1 = \vec{a} - \vec{b} + \vec{c}, \vec{r}_2 = \vec{b} + \vec{c} - \vec{a}, \vec{r}_3 = \vec{c} + \vec{a} + \vec{b}, \vec{r} = 2\vec{a} - 3\vec{b} + 4\vec{c}$. If $\vec{r} = \lambda_1 \vec{r}_1 + \lambda_2 \vec{r}_2 + \lambda_3 \vec{r}_3$, then
 (a) $\lambda_1 = 7$ (b) $\lambda_1 + \lambda_2 = 3$ (c) $\lambda_1 + \lambda_2 + \lambda_3 = 4$ (d) $\lambda_2 + \lambda_3 = 2$
16. If $\vec{p} = \lambda(\vec{u} \times \vec{v}) + \mu(\vec{v} \times \vec{w}) + \nu(\vec{w} \times \vec{u})$ and $[\vec{u} \vec{v} \vec{w}] = \frac{1}{5}$, then $\lambda + \mu + \nu$ is equal to
 (a) 5 (b) 10 (c) 15 (d) none of these
17. Two sides of a triangle are formed by the vectors $\vec{a} = 3\hat{i} + 6\hat{j} - 2\hat{k}$ and $\vec{b} = 4\hat{i} - \hat{j} + 3\hat{k}$. The angles of the triangle are
 (I) $\cos^{-1} \frac{7}{\sqrt{75}}$ (II) $\cos^{-1} \sqrt{\frac{26}{75}}$ (III) $\cos^{-1} \frac{3}{\sqrt{15}}$ (IV) $\cos^{-1} \frac{2}{3}$
 (a) I & III (b) II & III (c) III & IV (d) I & II
18. $(\vec{a} \times \hat{i}) + (\vec{a} \times \hat{j})^2 + (\vec{a} \times \hat{k})^2$ is equal to
 (a) \vec{a}^2 (b) $3\vec{a}^2$ (c) $2\vec{a}^2$ (d) none of these
19. If $\hat{i} \times (\vec{r} \times \hat{i}) + \hat{j} \times (\vec{r} \times \hat{j}) + \hat{k} \times (\vec{r} \times \hat{k}) = \vec{a} \times \vec{b}$ ($\vec{a} \neq 0, \vec{b} \neq 0$), then
 (a) $\vec{r} = \vec{a} \times \vec{b}$ (b) $\vec{r} = \frac{\vec{a} \times \vec{b}}{2}$ (c) $\vec{r} = \vec{0}$ (d) none of these
20. If $\vec{a} + \vec{b} + \vec{c} = \alpha \vec{d}, \vec{b} + \vec{c} + \vec{d} = \beta \vec{a}$, then $\vec{a} + \vec{b} + \vec{c} + \vec{d}$ is equal to

(a) $\beta\bar{b}$

(b) $\alpha\bar{a}$

(c) $\bar{0}$

(d) none of these

21. A five digit number is chosen at random. The probability that all the digit are distinct and digits at odd places are odd and digits at even place are even, is
- a) $\frac{1}{60}$ b) $\frac{2}{75}$ c) $\frac{1}{50}$ d) $\frac{1}{75}$
22. If two dice are thrown together, then the probability that the sum of numbers appearing on them is 9, is
- a) $\frac{1}{9}$ b) $\frac{1}{6}$ c) $\frac{1}{4}$ d) $\frac{1}{3}$
23. A man is known to speak truth in 75% cases. If he throws an unbiased die and tells his friend that it is a six, then the probability that it is actually a six, is
- a) $1/6$ b) $1/8$ c) $3/4$ d) $3/8$
24. A box contains 10 mangoes out of which 4 are rotten. 2 mangoes are taken out together. If one of them is found to be good, the probability that the other is also good is
- a) $1/3$ b) $8/15$ c) $5/13$ d) $2/3$
25. There are 4 white and 4 black balls in a bag and 3 balls are drawn at random. If balls of same colour are identical, the probability that none of them is black, is
- a) $1/4$ b) $1/14$ c) $1/2$ d) None of these

ANSWER KEY

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|---------|---------|---------|---------|---------|---------|---------|
| 1. (A) | 2. (A) | 3. (C) | 4. (A) | 5. (A) | 6. (A) | 7. (A) |
| 8. (D) | 9. (C) | 10. (D) | 11. (D) | 12. (B) | 13. (C) | 14. (B) |
| 15. (C) | 16. (D) | 17. (D) | 18. (C) | 19. (D) | 20. (C) | 21. (D) |
| 22. (A) | 23. (D) | 24. (C) | 25. (A) | | | |