

CLASS-12TH(MATHEMATICS) PAPER-1

1. The area bounded by $y = \sec^{-1} x$, $y = \operatorname{cosec}^{-1} x$ and $x - 1 = 0$ is

(A) $\left(\log(3 + 2\sqrt{2}) - \frac{\pi}{2}\right)$ sq. units

(B) $\left(\frac{\pi}{2} - \log(3 + 2\sqrt{2})\right)$ sq. units

(C) $(\pi - \log_e 3)$ sq. units

(D) None of these

Sol. []

2. The area of the loop of the curve, $ay^2 = x^2(a - x)$ is

(A) $4a^2$. Sq. units

(B) $\frac{8a^2}{15}$ sq. units

(C) $\frac{16a^2}{9}$ sq. units

(D) None of these

Sol. []

3. The area enclosed by the curves, $xy^2 = a^2(a - x)$ and $(a - x)y^2 = a^2x$ is

(A) $(\pi - 1)a^2$ sq. units

(B) $(4 - \pi)a^2$ sq. units

(C) $\pi a^2/3$ sq. units

(D) None of these

Sol. []

4. The gradient of the curve passing through the point (4, 0) is given by $\frac{dy}{dx} - \frac{y}{x} + \frac{5x}{(x+2)(x-3)} = 0$. If the point (5, a) lies on the curve, then the value of 'a' is

(A) $5 \ln \frac{7}{12}$

(B) $\frac{67}{12}$

(C) $5 \sin \frac{7}{12}$

(D) None of these

Sol. []

5. If for the differential equation $y' = \frac{y}{x} + \phi\left(\frac{x}{y}\right)$, the general solution is $y = \frac{x}{\log |Cx|}$, then $\phi(x/y)$ is given by

(A) $-x^2/y^2$

(B) y^2/x^2

(C) x^2/y^2

(D) $-y^2/x^2$

Sol. []

6. If $\phi(x)$ is a differentiable function, then the solution of the differential equation $dy + \{y\phi'(x) - \phi(x)\phi'(x)\}dx = 0$ is

(A) $y = \{\phi(x) - 1\} + ce^{-\phi(x)}$

(B) $y\phi(x) = \{\phi(x)\}^2 + c$

(C) $ye^{\phi(x)} = \phi(x)e^{\phi(x)} + c$

(D) $y - \phi(x) = \phi(x)e^{-\phi(x)}$

Sol. []

7. The position vector of P is

- (A) $\hat{i} - \hat{j} + 3\hat{k}$ (B) $\hat{i} - \hat{j}$ (C) $2\hat{i} - \hat{j} - 3\hat{k}$ (D) $\hat{i} + \hat{j} + 3\hat{k}$

Sol. []

8. The volume of tetrahedron ABCF is

- (A) $\frac{7}{3}$ cubic units (B) $\frac{7}{5}$ cubic units
(C) $\frac{3}{5}$ cubic units (D) 7 cubic units

Sol. []

9. The rectangle ABCD of dimension r and 2r is folded along diagonal BD such that planes ABD and CBD are perpendicular to each other, then the distance AC'' (in new position is)

- (A) $\sqrt{3}r$ (B) $\sqrt{85}r$ (C) $\sqrt{\frac{85}{5}}r$ (D) $\sqrt{\frac{17}{5}}r$

Sol. []

10. Suppose AB is a diameter of a circle and P is a plane through AB making an angle θ with the plane of the circle. If diameter of the circle be 2a, then the eccentricity of the curve of projection of the circle on P is

- (A) $\sin \theta$ (B) $\frac{2a \sin \theta}{1+a}$ (C) $\frac{a \sin \theta}{1+a}$ (D) $1 + \sin^2 \theta$

Sol. []

11. A plane makes intercepts OA, OB, OC whose measures are a, b, c on the axes OX, OY, OZ. The area of the triangle ABC is

- (A) $\sqrt{a^4 + b^4 + c^4 - a^2b^2 - b^2c^2 - c^2a^2}$ (B) $\frac{1}{2}\sqrt{a^2b^2 + b^2c^2 + c^2a^2}$
(C) $a^2 + b^2 + c^2 - bc - ca - ab$ (D) $\frac{1}{4}\sqrt{(a+b+c)(b+c+a)(c+a-b)(a+b-c)}$

Sol. []

Multiple choice Questions

12. Which of the following have the same bounded area ?

- (A) $f(x) = \sin x$, $g(x) = \sin^2 x$, where $0 \leq x \leq 10\pi$
(B) $f(x) = \sin x$, $g(x) = |\sin x|$, where $0 \leq x \leq 10\pi$
(C) $f(x) = |\sin x|$, $g(x) = \sin^3 x$, where $0 \leq x \leq 10\pi$
(D) $f(x) = \sin$, $g(x) = \sin 4x$, where $0 \leq x \leq 10\pi$

Sol. []

13. The differential equation $\frac{d^2x}{dy^2} + y + \cot^2 x = 0$ must be satisfied by

(A) $2 + c_1 \cos x + \sqrt{c_2} \sin x$

(B) $\cos x \cdot \ln\left(\tan \frac{x}{2}\right) + 2$

(C) $2 + c_1 \cos x + c_2 \sin x + \cos x \log\left(\tan \frac{x}{2}\right)$

(D) all the above

Sol. []

14. The curve for which the area of the triangle formed by the x-axis, the tangent line and radius vector of the point of tangency is equal to a^2 is

(A) $x = cy + \frac{a^2}{y}$

(B) $y = x - cx^2$

(C) $y = cx + \frac{a^2}{x}$

(D) $x = cy - \frac{a^2}{y}$

(where c is arbitrary constant)

Sol. []

15. The x-y plane is rotated about its line of intersection with the y-z plane by 45° , then the equation of the new plane is/are

(A) $z + x = 0$

(B) $z - y = 0$

(C) $x + y + z = 0$

(D) $z - x = 0$

Sol. []

Matrix

16. Column-I

Column-II

(A) If $\vec{a} + \vec{b} + \vec{c} = \alpha \vec{d}$, $\vec{b} + \vec{c} + \vec{d} = \beta \vec{a}$ and $\vec{a}, \vec{b}, \vec{c}$ are non-coplanar then $|\vec{a} + \vec{b} + \vec{c} + \vec{d}|$ is

(B) If \vec{a} and \vec{b} are unit vectors inclined at an angle θ to each other and $|\vec{a} + \vec{b}| < 1$, then θ can be equal to

(C) If \vec{a} units vector perpendicular to another unit vector \vec{b} then $|\vec{a} \times [\vec{a} \times \{\vec{a} \times (\vec{a} \times \vec{b})\}]|$ is equal to

(D) Let $\vec{a}, \vec{b}, \vec{c}$ be three unit vectors such that $\vec{a} + \vec{b} + \vec{c} = 0$, then the angle between \vec{a} and \vec{b} equal to

Sol. []

Integer Type

17. The are of the region bounded between the curves $|y| - |\sin| \geq 0$ and $x^2 + y - \pi^2 < 0$ is $\pi^3 - A$. Find the value of A.

Sol. []

18. If $14 + \ln k$ be the area bounded by the curves $|y| = e^{-|x|} - \frac{1}{2}$ and $\frac{|x| + |y|}{2} + \left| \frac{|x| - |y|}{2} \right| \leq 2$ then k is equal to

Sol. []

19. Area of the region bounded by the curve $y = \{x^2\}$, where $\{.\}$ denotes fractional part function $\forall x \in [-2, 2]$ is $p\left(\sqrt{q} + \sqrt{r} - \frac{7}{3}\right)$. Find the value of $p + q + r$.

Sol. []

20. Two point P and Q are given in the rectangular Cartesian co-ordinates on the curve $y = 2x+2$, such that $\overline{OP}\hat{i} = -1$ and $\overline{OQ}\hat{i} = 2$, where \hat{i} is a unit vector along the x-axis. The magnitude of the vector $\overline{OQ} - 4\overline{QP}$, is $2k$, where k equal.

Sol. []

21. If the ratio in which the plane $\vec{r} \cdot (\vec{r} - 2\vec{j} + 3\vec{k}) = 17$ divides the line joining the points $-2\vec{i} + 4\vec{j} + 7\vec{k}$ and $3\vec{i} - 5\vec{j} + 8\vec{k}$ is $\frac{a}{b}$, then $|a - b| =$

Sol. []